## Angles in Kites - Expert

1. Calculate the missing angle marked $x$.


Not drawn accurately
5. Calculate the missing angle marked $x$.


Not drawn accurately
9. Calculate the missing angle $\operatorname{marked} x$.


Not drawn accurately
10. Calculate the missing angle marked $y$.

3. Calculate the missing angle marked $x$.


Not drawn accurately
7. Calculate the missing angle marked $x$.


Not drawn accurately
marked $x$.

4. Calculate the value of $y$. Hence, find all the missing angles.


Not drawn accurately
8. Calculate the value of $x$. Hence, find all the missing angles.


Not drawn accurately
12. Calculate the missing angle marked $x$.


Not drawn accurately

## Angles in Kites - Expert Answers

| 1. $\begin{aligned} & x=(360-135-53) \div 2 \\ & x=86^{\circ} \end{aligned}$ | 2. $\begin{aligned} & y=360-120.5-120.5-70.25 \\ & y=48.75^{\circ} \end{aligned}$ | 3. $\begin{aligned} & x=360-117.2-117.2-62.7 \\ & x=62.9^{\circ} \end{aligned}$ | 4. $\begin{aligned} & 2 y+1+y+112+112=360 \\ & 3 y=135 \\ & y=45^{\circ} \end{aligned}$ <br> Missing angles are $112^{\circ}, 91^{\circ}$ and $45^{\circ}$ |
| :---: | :---: | :---: | :---: |
| 5. $\begin{aligned} & 360-318=42 \\ & (360-84-42) \div 2=117 \\ & x=360-117 \\ & x=243^{\circ} \end{aligned}$ | 6. $\begin{aligned} & y=360-116-116-94 \\ & y=34^{\circ} \end{aligned}$ | 7. $\begin{aligned} & 0.5 \times 68=34 \\ & x=(360-68-34) \div 2 \\ & x=129^{\circ} \end{aligned}$ | 8. $\begin{aligned} & 2 x-26+2 x-26+x+88 \\ & =360 \\ & 5 x=324 \\ & x=64.8^{\circ} \end{aligned}$ <br> Missing angles are $64.8^{\circ}$ and $103.6^{\circ}$ |
| 9. $\begin{aligned} & x=(360-35-35-25-25) \div 2 \\ & x=120^{\circ} \end{aligned}$ | $\begin{aligned} & \text { 10. } \\ & \begin{array}{l} 180-80=100 \\ y=360-100-100-75 \\ y=85^{\circ} \end{array} \end{aligned}$ | 11. $\begin{aligned} & x=180-100-45 \\ & x=35^{\circ} \end{aligned}$ | 12. $\begin{aligned} & 2 x+x+135+135=360 \\ & 3 x=90 \\ & x=30^{\circ} \end{aligned}$ |

## Angles in Mixed Quadrilaterals - Expert

1. Calculate the missing angles

marked $x$ and $y$. \begin{tabular}{l}
2. Calculate the value of $x$. Hence <br>
find all the missing angles.

 

3. Calculate the missing angle <br>
marked $x$.
\end{tabular}

## Angles in Mixed Quadrilaterals - Expert Answers

| 1. $\mathbf{3 6 0} \mathbf{- 2 1 4}=146^{\circ}$ $\begin{aligned} & x=180-146 \\ & x=34^{\circ} \end{aligned}$ $\begin{aligned} & y=180-63 \\ & y=117^{\circ} \end{aligned}$ | 2. $\begin{aligned} & 5 x-4+2 x+x+96=360 \\ & 8 x+92=360 \\ & 8 x=268 \\ & x=33.5^{\circ} \end{aligned}$ <br> Missing angles are $163.5^{\circ}$, $33.5^{\circ}$ and $67^{\circ}$ | $\text { 3. } \begin{aligned} x & =180-100-45 \\ x & =35^{\circ} \end{aligned}$ | 4. $\begin{aligned} & 35 \times 2=70 \\ & 2 x-3+2 x-3+2 x-3+2 x-3+ \\ & 35+35+35+35=360 \\ & 8 x=232 \\ & x=29 \\ & y=360-(4 \times 29-6) \\ & y=250^{\circ} \end{aligned}$ |
| :---: | :---: | :---: | :---: |
| 5. $\mathbf{1 8 0} \mathbf{- 1 2 5}=\mathbf{5} \mathbf{5}^{\circ}$ $\begin{aligned} & x=360-55 \\ & x=305^{\circ} \end{aligned}$ | $\text { 6. } \begin{aligned} & 3 a+b+a-3 b=180 \\ & 4 a-2 b=180 \\ & 3 a+b=110 \\ & \\ & a=40 \\ & b=-10 \end{aligned}$ | 7. $\mathbf{1 8 0}-\mathbf{6 8}=112^{\circ}$ $\begin{aligned} & 3 y+y+48+112+90=360 \\ & 4 y+250=360 \\ & 4 y=110 \\ & y=27.5 \end{aligned}$ <br> Missing angles are $112^{\circ}, 82.5^{\circ}$ and $75.5^{\circ}$ | $\text { 8. } \begin{aligned} 360-334=26^{\circ} \\ 360-132=228^{\circ} \\ 360-228-64-26=42 \\ \\ x=360-42 \\ x=318^{\circ} \end{aligned}$ |
| $\text { 9. } \begin{aligned} & 180-80=100 \\ & y=360-100-100-75 \\ & y=85^{\circ} \end{aligned}$ | $\text { 10. } \begin{aligned} & 360-318=42 \\ &(360-84-42) \div 2=117 \\ & x=360-117 \\ & x=243^{\circ} \end{aligned}$ | 11. $\begin{aligned} & 2 x+100+95+60=360 \\ & 2 x+255=360 \\ & 2 x=105 \\ & x=52.5^{\circ} \end{aligned}$ <br> Missing angle is $105^{\circ}$ | 12. $\begin{aligned} & 2 x+4+x+y+90=360 \\ & 3 x+y+94=360 \\ & 3 x+y=266 \\ & x+y+5=180 \\ & x+y=175 \\ & 2 x=91 \\ & x=45.5^{\circ} \\ & y=129.5^{\circ} \end{aligned}$ |

## Angles in Parallelograms - Expert



## Angles in Parallelograms - Expert Answers

| 1. $\begin{aligned} & x=180-64 \\ & x=116^{\circ} \\ & y=64^{\circ} \end{aligned}$ | 2. $\begin{aligned} & 180-77=103^{\circ} \\ & x=360-103 \\ & x=257^{\circ} \end{aligned}$ | 3. $\begin{aligned} & 180-125=55^{\circ} \\ & x=360-55 \\ & x=305^{\circ} \end{aligned}$ | 4. $\begin{aligned} & 4 x+110=180 \\ & 4 x=70 \\ & x=17.5 \\ & z=180-110 \\ & z=70^{\circ} \end{aligned}$ |
| :---: | :---: | :---: | :---: |
| 5. $\begin{aligned} & 2 x+3+x=180 \\ & 3 x=177 \\ & x=59^{\circ} \\ & y=59 \times 2+3 \\ & y=121^{\circ} \end{aligned}$ | 6. $\begin{aligned} & 2 x+12+5 x=180 \\ & 7 x=168 \\ & x=24 \end{aligned}$ <br> Missing angles are $120^{\circ}$ and $60^{\circ}$ | 7. $\begin{aligned} & 17 x-5+8 x=180 \\ & 25 x=185 \\ & x=7.4 \end{aligned}$ $\begin{aligned} & 8 \times 7.4+4 y=180 \\ & 4 y=120.8 \\ & y=30.2 \end{aligned}$ | 8. $\begin{aligned} & 180-105=75^{\circ} \\ & y+75=180 \\ & y=105^{\circ} \end{aligned}$ |
| 9. $\begin{aligned} & y=360-254 \\ & y=106^{\circ} \\ & 10 x+2+106=180 \\ & 10 x=72 \\ & x=7.2 \end{aligned}$ | 10. $\begin{aligned} & 5 x+3 x+4=180 \\ & 8 x=176 \\ & x=22 \end{aligned}$ <br> Missing angles are $110^{\circ}$ and $70^{\circ}$ | 11. $\begin{aligned} & 3 a+b+a-3 b=180 \\ & 4 a-2 b=180 \\ & 3 a+b=110 \\ & a=40 \\ & b=-10 \end{aligned}$ | 12. $\begin{aligned} & 5 y+115=180 \\ & 5 y=65 \\ & y=13 \end{aligned}$ $\begin{aligned} & 7 x-5=65 \\ & 7 x=70 \\ & x=10 \end{aligned}$ |

## Angles in Quadrilaterals - Expert

1. Calculate the missing angles marked $x$ and $y$.


Not drawn accurately
5. Calculate the missing angle marked $x$.


Not drawn accurately
9. Calculate the missing angle $\operatorname{marked} x$.


Not drawn accurately
2. Calculate the missing angles marked $x$ and $z$.


Not drawn accurately
6. Calculate the value of $x$. Hence, find the missing angle.


Not drawn accurately
10. Calculate the value of $x$. Hence, find all the missing angles.


Not drawn accurately
3. Calculate the missing angles marked $x$ and $y$.


Not drawn accurately
7. Calculate all the missing angles.


Not drawn accurately
11. Calculate the missing angle marked $x$.
 Not drawn accurately
4. Calculate the missing angle marked $x$.


Not drawn accurately
8. Calculate the value of $x$. Hence, find all the missing angles.


Not drawn accurately
12. Calculate the missing angle marked $x$.


Not drawn accurately

## Angles in Quadrilaterals - Expert Answers

| $\text { 1. } \begin{aligned} & 360-214=146^{\circ} \\ & x=180-146 \\ & x=34^{\circ} \\ & y=180-63 \\ & y=117^{\circ} \end{aligned}$ | $\text { 2. } \begin{gathered} 360-268=92^{\circ} \\ x=88^{\circ} \\ z=92^{\circ} \end{gathered}$ | $\text { 3. } \begin{aligned} x & =71^{\circ} \\ y & =180-71 \\ y & =109^{\circ} \end{aligned}$ | 4. $\mathbf{1 8 0}-\mathbf{5 8}=\mathbf{1 2 2}^{\circ}$ $\begin{aligned} & x=360-122-94-87 \\ & x=57^{\circ} \end{aligned}$ |
| :---: | :---: | :---: | :---: |
| 5. $\mathbf{1 8 0} \mathbf{- 1 2 1 = 5 9 ^ { \circ }}$ $\begin{aligned} & x=360-100-84-59 \\ & x=117^{\circ} \end{aligned}$ | 6. $2 x+100+95+60=\mathbf{3 6 0}$ $\begin{aligned} & 2 x+255=360 \\ & 2 x=105 \\ & x=52.5^{\circ} \end{aligned}$ <br> Missing angle is $105^{\circ}$ | 7. $\mathbf{1 8 0}-\mathbf{6 8}=11 \mathbf{2}^{\circ}$ $\begin{aligned} & 3 y+y+48+112+90=360 \\ & 4 y+250=360 \\ & 4 y=110 \\ & y=27.5 \end{aligned}$ <br> Missing angles are $112^{\circ}$, $82.5^{\circ}$ and $75.5^{\circ}$ | 8. $\begin{aligned} & 5 x-5+2 x+3 x+90=360 \\ & 10 x+85=360 \\ & 10 x=275 \\ & x=27.5 \end{aligned}$ <br> Missing angles are $132.5^{\circ}$, $55^{\circ}, 82.5^{\circ}$ |
| $\text { 9. } \begin{aligned} & 180-90=90^{\circ} \\ & 360-148=212^{\circ} \\ & 180-151=29^{\circ} \\ & x=360-212-90-29 \\ & x=29^{\circ} \end{aligned}$ | $\text { 10. } \begin{aligned} & 5 x-4+2 x+x+96=360 \\ & 8 x+92=360 \\ & 8 x=268 \\ & x=33.5^{\circ} \end{aligned}$ <br> Missing angles are $163.5^{\circ}$, $33.5^{\circ}$ and $67^{\circ}$ | $\text { 11. } \begin{aligned} & 360-334=26^{\circ} \\ & 360-132=228^{\circ} \\ & 360-228-64-26=42 \\ & x=360-42 \\ & x=318^{\circ} \end{aligned}$ | $\text { 12. } \begin{aligned} & 2 x+4+x+y+90=360 \\ & 3 x+y+94=360 \\ & 3 x+y=266 \\ & x+y+5=180 \\ & x+y=175 \\ & \\ & 2 x=91 \\ & x=45.5^{\circ} \\ & y=129.5^{\circ} \end{aligned}$ |

## Angles in Rhombuses - Expert

1. Calculate the value of $x$. Hence,

find all the missing angles. \begin{tabular}{l}
Calculate the value of $x$. Hence, <br>
find all the missing angles.

 

3. Calculate the missing angles <br>
marked $x, y$ and $z$.
\end{tabular}

## Angles in Rhombuses - Expert Answers

| 1. $3 x+x+3 x+x=360$ $\begin{aligned} & 8 x=360 \\ & x=45^{\circ} \end{aligned}$ <br> Missing angles are $45^{\circ}, 45^{\circ}$, $135^{\circ}$ and $135^{\circ}$ | 2. $5 x-6+x+5 x-6+x=360$ $\begin{aligned} & 12 x=372 \\ & x=31^{\circ} \end{aligned}$ <br> Missing angles are $31^{\circ}, 31^{\circ}$, $149^{\circ}$ and $149^{\circ}$ | $\text { 3. } \begin{aligned} x & =123^{\circ} \\ y & =(360-123-123) \div 2 \\ y & =57^{\circ} \\ z & =360-57 \\ z & =303^{\circ} \end{aligned}$ | 4. $\begin{aligned} & x=132^{\circ} \\ & y=(360-132-132) \div 2 \\ & y=48^{\circ} \\ & z=360-48 \\ & z=312^{\circ} \end{aligned}$ |
| :---: | :---: | :---: | :---: |
| $\text { 5. } \begin{aligned} & 360-307=53^{\circ} \\ & (360-53-53) \div 2=127^{\circ} \\ & x=360-127 \\ & x=233^{\circ} \end{aligned}$ | 6. $\mathbf{3 6 0}-\mathbf{2 9 9}=\mathbf{6 1}{ }^{\circ}$ $\begin{aligned} & (360-61-61) \div 2=119^{\circ} \\ & y=360-119 \\ & y=241^{\circ} \end{aligned}$ | 7. $\begin{aligned} & 23 x-5+14 x+110+70=360 \\ & 37 x=185 \\ & x=5 \end{aligned}$ <br> Or, solve to find the opposite angle. $\begin{aligned} & 23 x-5=110 \\ & 23 x=115 \\ & x=5 \end{aligned}$ | $\text { 8. } \begin{aligned} & 6 x+2 x+6 x+2 x=360 \\ & 16 x=360 \\ & x=22.5 \end{aligned}$ |
| 9. $\begin{aligned} & x=115^{\circ} \\ & 2 y+2 y+115+115=360 \\ & 4 y=130 \\ & y=32.5 \\ & z=360-(32.5 \times 2) \\ & z=295^{\circ} \end{aligned}$ | $\text { 10. } \begin{aligned} 40 & \times 2=80 \\ x & =(360-80-80) \div 2 \\ x & =100^{\circ} \\ y & =360-100 \\ y & =260^{\circ} \end{aligned}$ | 11. $26 \times 2=52$ $\begin{aligned} & 5 x-2+5 x-2+52+52=360 \\ & 10 x=260 \\ & x=26 \\ & y=360-(5 \times 26-2) \\ & y=232^{\circ} \end{aligned}$ | $\text { 12. } 35 \times 2=70 \text { } \begin{aligned} & 2 x-3+2 x-3+2 x-3+2 x-3+ \\ & 35+35+35+35=360 \\ & 8 x=232 \\ & x=29 \\ & y=360-(4 \times 29-6) \\ & y=250^{\circ} \end{aligned}$ |

## Colour by Number: Angles in Quadrilaterals - Expert

Each question gives information about the interior angles of a quadrilateral. Calculate the value of $x$ then use the key to shade the section in the correct colour.

| Black | Orange | Cream | Brown | Dark Green | Green | Light Green |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Less than <br> $30^{\circ}$ | $30^{\circ}$ to $45^{\circ}$ | $46^{\circ}$ to $65^{\circ}$ | $66^{\circ}$ to $89^{\circ}$ | Right angle | $91^{\circ}$ to $200^{\circ}$ | More than <br> $200^{\circ}$ |



## Question

| 1. | right angle, $2 x-50^{\circ}, 71^{\circ}, 57^{\circ}$ |
| ---: | :--- |
| 2. | $x-72^{\circ}, x-72^{\circ}, 57^{\circ}, 45^{\circ}$ |
| 3. | $2 x-100^{\circ}, 18^{\circ}, 32^{\circ}, 8^{\circ}$ |
| 4. | $196^{\circ}, 2 x, x, 68^{\circ}$ |
| 5. | $x+10^{\circ}, x+10^{\circ}, 118^{\circ}, 118^{\circ}$ |
| 6. | right angle, $15^{\circ}, 30^{\circ}, x$ |
| 7. | $3 x-26^{\circ}$, right angle, $5^{\circ}, 12^{\circ}$ |
| 8. | $4 x$ |
| 9. | $215^{\circ}, 75^{\circ}, 38^{\circ}, x$ |
| 10. | $x+61^{\circ}, x+61^{\circ}, 36^{\circ}, 10^{\circ}$ |
| 11. | right angle, $135^{\circ}, 45^{\circ}, x$ |
| 12. | $142^{\circ}, x, 100^{\circ}, 30^{\circ}$ |
|  |  |


| 13. | $2 x+5^{\circ}, 2 x+5^{\circ}, 81^{\circ}, 81^{\circ}$ |
| :--- | :--- |
| 14. | $175^{\circ}, 111^{\circ}, 43^{\circ}, x$ |
| 15. | right angle, $212^{\circ}, 38^{\circ}, x$ |
| 16. | $3 x-50^{\circ}, 65^{\circ}, 51^{\circ}, 24^{\circ}$ |
| 17. | $95^{\circ}, 95^{\circ}, x, x$ |
| 18. | $2 x, 2 x, 100^{\circ}, 100^{\circ}$ |
| 19. | right angle, $123^{\circ}, 79^{\circ}, x$ |
| 20. | $3 x-4^{\circ}, 3 x-4^{\circ}, 43^{\circ}, 43^{\circ}$ |
| 21. | $2 x-15^{\circ}, 2 x-15^{\circ}, 13^{\circ}, 13^{\circ}$ |
| 22. | $125^{\circ}, 125^{\circ}, x, x$ |
| 23. | $104^{\circ}, 42^{\circ}, 58^{\circ}, x$ |
| 24. | $153^{\circ}, 153^{\circ}, 10^{\circ}, x$ |
| 25. | $114^{\circ}, 32^{\circ}, 23^{\circ}, x$ |
| 26. | $156^{\circ}, 100^{\circ}, 14^{\circ}, x$ |
| 27. | $36^{\circ}, 51^{\circ}, 23^{\circ}, x$ |
| 28. | right angle, $97^{\circ}, 84^{\circ}, x$ |
| 29. | $61^{\circ}, 35^{\circ}, 172^{\circ}, x$ |
| 30. | $105^{\circ}, 105^{\circ}, 98^{\circ}, x$ |
| 31. | $x-56^{\circ}, x-56^{\circ}, 34^{\circ}, 34^{\circ}$ |
| 32. | $x+7^{\circ}, x+77^{\circ}, 88^{\circ}, 88^{\circ}$ |
| 33. | $2 x-15^{\circ}, 2 x-15^{\circ}, 21^{\circ}, 9^{\circ}$ |
| 34. | $x-12^{\circ}, x-12^{\circ}, 111^{\circ}, 111^{\circ}$ |
| 35. | $2 x-8^{\circ}, 2 x-8^{\circ}, 38^{\circ}, 38^{\circ}$ |
| 36. | $115^{\circ}, 115^{\circ}, x, x$ |
| 37. | $75^{\circ}, 48^{\circ}, 39^{\circ}, x$ |
| 38. | $115^{\circ}, 57^{\circ}, 96^{\circ}, x$ |
| 39. | $107^{\circ}, 100^{\circ}, 65^{\circ}, x$ |
| 40. | $120^{\circ}, 120^{\circ}, x, x$ |
| 41. | $152^{\circ}, 60^{\circ}, 64^{\circ}, x$ |
| 42. | $2 x-350^{\circ}, 2 x-350^{\circ}, 110^{\circ}, 110^{\circ}$ |
| 43. | $150^{\circ}, 150^{\circ}, 45^{\circ}, x$ |
| 44. | $5 x-4^{\circ}, 5 x-4^{\circ}, 58^{\circ}, 10^{\circ}$ |
| 45. | $92^{\circ}, 92^{\circ}, x, x$ |
| 46. | $2 x+10^{\circ}, 2 x+10^{\circ}, 146^{\circ}, 70^{\circ}$ |
| 47. | $112^{\circ}, 95^{\circ}, 64^{\circ}, x$ |
| 48. | $2 x-35^{\circ}, 2 x-35^{\circ}, 56^{\circ}, 14^{\circ}$ |
| 49. | $x+17^{\circ}, x+17^{\circ}, 98^{\circ}, 48^{\circ}$ |
| 50. | $95^{\circ}, 101^{\circ}, 72^{\circ}, x$ |
|  |  |

## Colour by Number: Angles in Quadrilaterals - Expert Answers

Each question gives information about the interior angles of a quadrilateral. Calculate the value of $x$ then use the key to shade the section in the correct colour.

| Black | Orange | Cream | Brown | Dark Green | Green | Light Green |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Less than <br> $30^{\circ}$ | $30^{\circ}$ to $45^{\circ}$ | $46^{\circ}$ to $65^{\circ}$ | $66^{\circ}$ to $89^{\circ}$ | Right angle | $91^{\circ}$ to $200^{\circ}$ | More than <br> $200^{\circ}$ |



|  | Colour | Question |
| ---: | :--- | :--- |
| 1. |  | right angle, $2 x-50^{\circ}, 71^{\circ}, 57^{\circ}$ |
| 2. |  | $x-72^{\circ}, x-72^{\circ}, 57^{\circ}, 45^{\circ}$ |
| 3. |  | $2 x-100^{\circ}, 18^{\circ}, 32^{\circ}, 8^{\circ}$ |
| 4. |  | $196^{\circ}, 2 x, x, 68^{\circ}$ |
| 5. |  | $x+10^{\circ}, x+10^{\circ}, 118^{\circ}, 118^{\circ}$ |
| 6. |  | right angle, $15^{\circ}, 30^{\circ}, x$ |
| 7. |  | $3 x-26^{\circ}$, right angle, $5^{\circ}, 12^{\circ}$ |
| 8. |  | $4 x$ |
| 9. |  | $215^{\circ}, 75^{\circ}, 38^{\circ}, x$ |
| 10. |  | $x+61^{\circ}, x+61^{\circ}, 36^{\circ}, 10^{\circ}$ |
| 11. |  | right angle, $135^{\circ}, 45^{\circ}, x$ |
| 12. |  | $142^{\circ}, x, 100^{\circ}, 30^{\circ}$ |


| 13. |  | $2 x+5^{\circ}, 2 x+5^{\circ}, 81^{\circ}, 81^{\circ}$ |
| :---: | :---: | :---: |
| 14. |  | $175^{\circ}, 111^{\circ}, 43^{\circ}, x$ |
| 15. |  | right angle, $212^{\circ}, 38^{\circ}, x$ |
| 16. |  | $3 x-50^{\circ}, 65^{\circ}, 51^{\circ}, 24^{\circ}$ |
| 17. |  | 95 ${ }^{\circ}, 95^{\circ}, x, x$ |
| 18. |  | $2 x, 2 x, 100^{\circ}, 100^{\circ}$ |
| 19. |  | right angle, $123^{\circ}, 79^{\circ}, x$ |
| 20. |  | $3 x-4^{\circ}, 3 x-4^{\circ}, 43^{\circ}, 43^{\circ}$ |
| 21. |  | $2 x-15^{\circ}, 2 x-15^{\circ}, 13^{\circ}, 13^{\circ}$ |
| 22. |  | $125^{\circ}, 125^{\circ}, x, x$ |
| 23. |  | $104^{\circ}, 42^{\circ}, 58^{\circ}, x$ |
| 24. |  | $153^{\circ}, 153^{\circ}, 10^{\circ}, x$ |
| 25. |  | $114^{\circ}, 32^{\circ}, 23^{\circ}, x$ |
| 26. |  | $156^{\circ}, 100^{\circ}, 14^{\circ}, x$ |
| 27. |  | $36^{\circ}, 51^{\circ}, 23^{\circ}, x$ |
| 28. |  | right angle, $97^{\circ}, 84^{\circ}, x$ |
| 29. |  | $61^{\circ}, 35^{\circ}, 172^{\circ}, x$ |
| 30. |  | $105^{\circ}, 105^{\circ}, 98^{\circ}, x$ |
| 31. |  | $x-56^{\circ}, x-56^{\circ}, 34^{\circ}, 34^{\circ}$ |
| 32. |  | $x+7^{\circ}, x+7^{\circ}, 88^{\circ}, 88^{\circ}$ |
| 33. |  | $2 x-15^{\circ}, 2 x-15^{\circ}, 21^{\circ}, 9^{\circ}$ |
| 34. |  | $x-12^{\circ}, x-12^{\circ}, 111^{\circ}, 111^{\circ}$ |
| 35. |  | $2 x-8^{\circ}, 2 x-8^{\circ}, 38^{\circ}, 38^{\circ}$ |
| 36. |  | $115^{\circ}, 115^{\circ}, x, x$ |
| 37. |  | $75^{\circ}, 48^{\circ}, 39^{\circ}, x$ |
| 38. |  | $115^{\circ}, 57^{\circ}, 96^{\circ}, x$ |
| 39. |  | $107^{\circ}, 100^{\circ}, 65^{\circ}, x$ |
| 40. |  | $120^{\circ}, 120^{\circ}, x, x$ |
| 41. |  | $152^{\circ}, 60^{\circ}, 64^{\circ}, x$ |
| 42. |  | $2 x-350^{\circ}, 2 x-350^{\circ}, 110^{\circ}, 110^{\circ}$ |
| 43. |  | $150^{\circ}, 150^{\circ}, 45^{\circ}, x$ |
| 44. |  | $5 x-4^{\circ}, 5 x-4^{\circ}, 58^{\circ}, 10^{\circ}$ |
| 45. |  | $92^{\circ}, 92^{\circ}, x, x$ |
| 46. |  | $2 x+10^{\circ}, 2 x+10^{\circ}, 146^{\circ}, 70^{\circ}$ |
| 47. |  | $112^{\circ}, 95^{\circ}, 64^{\circ}, x$ |
| 48. |  | $2 x-35^{\circ}, 2 x-35^{\circ}, 56^{\circ}, 14^{\circ}$ |
| 49. |  | $x+17^{\circ}, x+17^{\circ}, 98^{\circ}, 48^{\circ}$ |
| 50. |  | $95^{\circ}, 101^{\circ}, 72^{\circ}, x$ |

## Angles in Quadrilaterals - Essential

Solve the clues to find the four-digit code to escape the classroom!

1. Calculate the value of $x$.


Not drawn accurately.
3. Calculate the value of the missing angle marked $x$.


4. Calculate the value of $y$.


Not drawn accurately

The first digit of the code is given by the tenths in the value of $x$ in question 1 . The second digit is given by the tens digit in the answer to question 2. The third digit is given by the sum of the digits of angle $x$ in question 3 . The fourth digit is the sum of the digits of $y$ in question 4.


## Angles in Quadrilaterals - Essential

Solve the clues to find the four-digit code to escape the classroom!

1. Calculate the value of $x$.

2. Calculate the value of the missing angle marked $x$.


3. Calculate the value of $y$.


Not drawn accurately.

The first digit of the code is given by the tenths in the value of $x$ in question 1 . The second digit is given by the tens digit in the answer to question 2. The third digit is given by the sum of the digits of angle $x$ in question 3 . The fourth digit is the sum of the digits of $y$ in question 4.

## Angles in Quadrilaterals - Essential Answers

Solve the clues to find the four-digit code to escape the classroom!

1. Calculate the value of $x$.


Not drawn accurately.
3. Calculate the value of the missing angle marked $x$.


Not drawn accurately.

4. Calculate the value of $y$.


Not drawn accurately.

The first digit of the code is given by the tenths in the value of $x$ in question 1 . The second digit is given by the tens digit in the answer to question 2. The third digit is given by the sum of the digits of angle $x$ in question 3 . The fourth digit is the sum of the digits of $y$ in question 4.

| 1. $\mathbf{3 6 0} \mathbf{- 2 4 5}=\mathbf{1 1 5}{ }^{\circ}$ $y=115^{\circ}$ $\begin{aligned} & 8 x+5+115=180 \\ & 8 x=60 \\ & x=7.5 \end{aligned}$ | $\text { 2. } \begin{aligned} & 5 x+x+5 x+x=360 \\ & 12 x=360 \\ & x=30^{\circ} \end{aligned}$ |
| :---: | :---: |
| $\text { 3. } \begin{aligned} x & =360-112-112-35 \\ x & =101^{\circ} \end{aligned}$ | $\begin{aligned} & \text { 4. } 180-70=110^{\circ} \\ & 4 y+y+57+90+110=360 \\ & 5 y=103 \\ & y=20.6 \end{aligned}$ |

Exit Code: 5328

## Angles in Quadrilaterals - Expert

Solve the clues to find the four-digit code to escape the classroom!

1. Calculate the missing angle marked $x$.


Not drawn accurately.
3. Calculate the value of $x$.


Not drawn accurately.
2. Calculate the missing angles marked $x$ and $y$ in the rhombus.

4. Calculate the value of $x$.


Not drawn accurately.

The first digit of the code is given by the sum of the digits for angle $x$ in question 1. The second digit is given by the units for both $x$ and $y$ in question 2 . The third digit is given by the tens in the value for $x$ in question 3. The fourth digit is given by the units in the value for $x$ in question 4.

## Angles in Quadrilaterals - Expert

Solve the clues to find the four-digit code to escape the classroom!

1. Calculate the missing angle marked $x$.


Not drawn accurately.
3. Calculate the value of $x$.


Not drawn accurately.
2. Calculate the missing angles marked $x$ and $y$ in the rhombus.

4. Calculate the value of $x$.


Not drawn accurately.

The first digit of the code is given by the sum of the digits for angle $x$ in question 1. The second digit is given by the units for both $x$ and $y$ in question 2 . The third digit is given by the tens in the value for $x$ in question 3. The fourth digit is given by the units in the value for $x$ in question 4 .


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## Angles in Quadrilaterals - Expert Answers

Solve the clues to find the four-digit code to escape the classroom!

1. Calculate the missing angle marked $x$.


Not drawn accurately.
3. Calculate the value of $x$.


Not drawn accurately.
2. Calculate the missing angles marked $x$ and $y$ in the rhombus.

4. Calculate the value of $x$.


Not drawn accurately.

The first digit of the code is given by the sum of the digits for angle $x$ in question 1. The second digit is given by the units for both $x$ and $y$ in question 2 . The third digit is given by the tens in the value for $x$ in question 3. The fourth digit is given by the units in the value for $x$ in question 4.

| 1. $\mathbf{3 6 0}-\mathbf{3 2 0}=\mathbf{4 0}{ }^{\circ}$ $\begin{aligned} & (360-82-40) \div 2=119^{\circ} \\ & x=360-119 \\ & x=241^{\circ} \end{aligned}$ | $\text { 2. } \begin{aligned} & 50 \times 2=100^{\circ} \\ & x=(360-100-100) \div 2 \\ & x=80^{\circ} \\ & y=360-80 \\ & y=280^{\circ} \end{aligned}$ |
| :---: | :---: |
| $\text { 3. } 5 x-15+10 x=180 ~ 子 \begin{aligned} & 15 x=195 \\ & x=13 \end{aligned}$ | $\text { 4. } \begin{aligned} & 2 x+x+49+38=360 \\ & 3 x=273 \\ & x=91^{\circ} \end{aligned}$ |

Exit Code: 7011

## Angles in Quadrilaterals



## Irregular Trapezium

## Properties:

- The interior angles add up to $360^{\circ}$.
- Each angle may be different
- It has 1 pair of parallel lines
- It has 2 pairs of angles that are supplementary: they add up to $180^{\circ}$.


Isosceles Trapezium

## Properties:

- The interior angles add up to $360^{\circ}$.
- It has 1 pair of parallel lines.
- There are 2 pairs of angles that are equal.
- Both pairs of opposite angles are
supplementary: they add up to $180^{\circ}$.



## Square

## Properties:

- The interior angles add up to $360^{\circ}$.
- Each angle is $90^{\circ}$
- All sides have equal length.
- It has 2 pairs of parallel lines.



## Rhombus

## Properties:

- The interior angles add up to $360^{\circ}$.
- All sides have equal length.
- Opposite sides are parallel and opposite angles are equal.
- The diagonals bisect each other at a right angle.



## Kite

## Properties:

- The interior angles add up to $360^{\circ}$.
- There are 2 congruent pairs of sides.
- Each pair consists of 2 equal-length sides that are adjacent (they meet).
- The angles are equal where the 2 pairs meet.
- The diagonals are perpendicular


Parallelogram

## Properties:

- The interior angles add up to $360^{\circ}$.
- Opposite sides are parallel.
- Opposite sides are equal in length.
- Opposite angles are equal (angles $a$ are the same and angles $b$ are the same).
- Angles $a$ and $b$ are supplementary: they add up to $180^{\circ}$.


## Angles in Quadrilaterals



## Irregular Trapezium

## Properties:

- The interior angles add up to $360^{\circ}$.
- Each angle may be different.
- It has 1 pair of parallel lines.
- It has 2 pairs of angles that are supplementary: they add up to $180^{\circ}$.


## Angles in Quadrilaterals



## Square

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- The interior angles add up to $360^{\circ}$.
- Each angle is $90^{\circ}$.
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## Angles in Quadrilaterals



## Kite

## Properties:

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## Angles in Quadrilaterals



## Isosceles Trapezium

## Properties:

- The interior angles add up to $360^{\circ}$.
- It has 1 pair of parallel lines.
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## Angles in Quadrilaterals



## Rhombus

## Properties:

- The interior angles add up to $360^{\circ}$.
- All sides have equal length.
- Opposite sides are parallel and opposite angles are equal.
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## Angles in Quadrilaterals



## Parallelogram

## Properties:

- The interior angles add up to $360^{\circ}$.
- Opposite sides are parallel.
- Opposite sides are equal in length.
- Opposite angles are equal (angles $a$ are the same and angles $b$ are the same).
- Angles $a$ and $b$ are supplementary: they add up to $180^{\circ}$.

Angle Properties
Angles in
Quadrilaterals: Expert Level



## Starter Task

Think, Pair, Share

Write down the definition of a quadrilateral.

A quadrilateral is a twodimensional, four-sided shape which is closed (the lines join up) and has straight sides.

List some of the properties of a quadrilateral.

- four sides (edges)
- four corners (vertices)
- interior angles that add up to $360^{\circ}$

List some examples of quadrilaterals.

Some examples include square, rectangle, trapezium, rhombus, parallelogram and kite.

Draw an example of a quadrilateral.


## Quadrilaterals

A quadrilateral is a two-dimensional, four-sided shaped which is closed (the lines join up) and has straight sides.

The interior angles of a quadrilateral always sum to $360^{\circ}$.

## Quadrilaterals

Using the angles in each question, decide whether it is a quadrilateral or not.

|  | Quadrilateral | Not a Quadrilateral |
| :---: | :---: | :---: |
| $56^{\circ}, 131^{\circ}, 95^{\circ}, 108^{\circ}$ |  | $\mathbf{X}$ |
| $90^{\circ}, 160^{\circ}, 75^{\circ}, 35^{\circ}$ | $\boldsymbol{\imath}$ |  |
| $115^{\circ}, 37^{\circ}, 185^{\circ}, 23^{\circ}$ | $\boldsymbol{\lambda}$ |  |
| $237^{\circ}, 102^{\circ}, 14^{\circ}, 7^{\circ}$ | $\boldsymbol{\imath}$ |  |
| $96^{\circ}, 48^{\circ}, 145^{\circ}, 72^{\circ}$ |  |  |
| $116^{\circ}, 116^{\circ}, 98^{\circ}, 30^{\circ}$ | $\boldsymbol{\gamma}$ | $\mathbf{X}$ |

## Types of Quadrilaterals



## Square

The interior angles add up to $360^{\circ}$.
Each angle is $90^{\circ}$.
All sides have equal length.
It has 2 pairs of parallel lines.

## Types of Quadrilaterals



## Rectangle

The interior angles add up to $360^{\circ}$.
Each angle is $90^{\circ}$.
It has 2 pairs of equal angles.
It has 2 pairs of parallel lines.

## Types of Quadrilaterals



## Irregular Trapezium

The interior angles add up to $360^{\circ}$.
Each angle may be different.
It has 1 pair of parallel lines.
It has 2 pairs of angles that are supplementary: they add up to $180^{\circ}$.

## Types of Quadrilaterals

## Isosceles Trapezium

The interior angles add up to $360^{\circ}$.
It has 1 pair of parallel lines.
There are 2 pairs of angles that are equal.

Both pairs of opposite angles are supplementary: they add up to $180^{\circ}$.

## Types of Quadrilaterals

## Rhombus

The interior angles add up to $360^{\circ}$.
All sides have equal length.
Opposite sides are parallel and opposite angles are equal.

The diagonals bisect each other at right angle.

## Types of Quadrilaterals

## Parallelogram



The interior angles add up to $360^{\circ}$.
Opposite sides are parallel.
Opposite sides are equal in length
Opposite angles are equal (angles a are the same and angles $b$ are the same).

Angles a and bare supplementary: they add up to $180^{\circ}$.

## Types of Quadrilaterals

## Kite



The interior angles add up to $360^{\circ}$.
There are 2 congruent pairs of sides.
Each pair consists of 2 equal-length sides that are adjacent (they meet).

The angles are equal where the 2 pairs meet.

The diagonals are perpendicular.

## Finding Missing Angles in Quadrilaterals

Find the value of $x$. Hence, find all the missing angles.

$6 x-3+2 x+x+111=360$
$9 x=252$
$\mathrm{x}=28^{\circ}$
Missing angles are $28^{\circ}, 56^{\circ}$ and $165^{\circ}$

## Finding Missing Angles in Quadrilaterals

Find the value of $x$. Hence, find all the missing angles.

$5 x+2+4 x+x+98=360$
$10 x=260$
$x=26^{\circ}$
Missing angles are $26^{\circ}, 104^{\circ}$ and $132^{\circ}$

## Finding Missing Angles in Quadrilaterals

Find the value of $x$. Hence, find all the missing angles.
$3 x-32+3 x-32+x+67=360$

$7 x=357$
$x=51^{\circ}$
Missing angles are $51^{\circ}, 121^{\circ}$ and $121^{\circ}$

## Finding Missing Angles in Quadrilaterals

Find the value of $x$. Hence, find all the missing angles. Give a reason for each stage of your working.


180-126 = $54^{\circ}$
$2 x-15+3 x+x+54=360$
$6 x=321$
$x=53.5^{\circ}$
Missing angles are $54^{\circ}, 53.5^{\circ}, 160.5^{\circ}$ and $92^{\circ}$

## Plenary

1 example of how to find a missing angle in a quadrilateral

2 properties of quadrilaterals I must remember

## 3 quadrilaterals I know

## Escape the Room

## Angles in Quadrilaterals - Essential

Solve the clues to find the four-digit code to escape the classroom

4. Calculate the value of $y$.

Nof drown accurately.

[^0]
## Angles in Quadrilaterals - Expert

Solve the clues to find the four-digit code to escape the classroom:

1. Calculate the missing angle
marked $x$



> The first digit of the code is given by the sum of the digits for angle $x$ in question 1 . The second digit is giver by the units for both r and $y$ in question 2 . The third digit is given by the tens in the value for $x$ in question 3. The fourth digit is given by the unts in the value to $x$ in question 4.




## Angles in Quadrilaterals Teaching Ideas

## Learning Objective:

To identify and find missing angles in quadrilaterals.
Targeting Assessment
Objectives AO1 and AO2.

## Success Criteria:

- To recall the key properties of different quadrilaterals.
- To use an angle rule to find a missing value.
- Form and solve equations using knowledge of angle facts.


## Context

This lesson aims to secure students' understanding of how to find missing angles in a range of quadrilaterals. The lesson aims to extend students' learning by requiring them to use an algebraic method to find the missing angles in a quadrilateral. Therefore, they should have a good understanding of how to calculate angles on a straight line and about a point as well as how to form and solve equations (including a few simultaneous equations for additional challenge).

## Resources

- PowerPoint
- Angles in Quadrilaterals
- Colour by Number
- Angles in Quadrilaterals Posters
- Angles in Kites
- Escape the Room - Essential
- Escape the Room - Expert
- Angles in Rhombuses
- Angles in Parallelograms
- Angles in Mixed Quadrilaterals


## Starter

## Think, Pair, Share

Display the ‘Think, Pair, Share’ questions. Allow students approximately 5 minutes to discuss their ideas with a partner. They could record their answers in books or mini-whiteboards.

## Main Activities

## Quadrilaterals

Once the starter is completed, draw the class together to talk through their ideas. Using the following slide, share the main teaching point that interior angles of a quadrilateral always add up to 360 degrees. Students should record this in their books. Following this, students are asked to apply their understanding to decide whether the angles make a quadrilateral or not. When asking for the answers, ensure you clarify students' understanding by asking them why it can't be a quadrilateral. Answers should be focusing on the interior angles in a quadrilateral adding up to 360 degrees.

## Types of Quadrilaterals

The following slides go through each key quadrilateral and share the key properties for each. These are also available as posters if you don't wish for students to copy down from the board. You could also refer to the images on each slide when discussing the properties to highlight them.

## Finding Missing Angles in Quadrilaterals

All the examples are designed to guide students on how to calculate the missing angle in a quadrilateral. Each slide provides a question followed by the calculations broken down into simple steps. You may wish to simply display the question and ask students for suggestions for the missing angles via whole class discussion. Alternatively, you may wish for students to work independently on the questions and display their answers on mini-whiteboards. Either way, encourage students to use the angle rule (that the angles in a quadrilateral add up to 360 degrees) to justify their answer by asking them, 'why is your answer correct?' 'Why can't the answer be something else?' You may wish for students to record their answers and calculations in their books.

Following this, students have the option of completing a range of Angles in Quadrilaterals Worksheets. They can focus on a particular quadrilateral or they may wish to complete the mixed quadrilateral sheet. Alternatively, students may also choose the Colour by Number activity to help them practise finding missing angles in quadrilaterals.

## Plenary

The plenary draws the lesson together by asking students to reflect on their learning during the lesson. Allow students enough time to complete the three questions. Use your best judgement to decide whether students share what they've written with the class or whether you will read them afterwards.

## Escape the Room

Escape the Room requires students to find missing angles in four quadrilaterals to find a code to 'exit' the room at the end of the lesson. These are differentiated at two different levels. You may wish for students to pass you their answers on leaving the classroom as they may provide you with immediate information that you can use to assess students' understanding and provide insight for subsequent lessons.


[^0]:    The first digit of the code is given by the tentits in the value of $x$ in question 1. The second digit is given by the tens digit in the answer to question 2 . The third digit is given by the sum of the digits of angle. $x$ in question 3 . The fourth digit is the sum of the digits of $y$ in question 4

