### **Angles in Kites - Expert**



### Angles in Kites - Expert **Answers**

1.	2.	3.	4.
x = (360 - 135 - 53) ÷ 2 x = 86°	y = 360 - 120.5 - 120.5 - 70.25 y = 48.75°	x = 360 - 117.2 - 117.2 - 62.7 x = 62.9°	2y + 1 + y + 112 + 112 = 360 3y = 135 $y = 45^{\circ}$
			Missing angles are 112°, 91° and 45°
5.	6.	7.	8.
360 - 318 = 42	<i>y</i> = 360 – 116 – 116 – 94	0.5 × 68 = 34	2x - 26 + 2x - 26 + x + 88
(360 - 84 - 42) ÷ 2 = 117	$y = 34^{\circ}$	r = (360 - 68 - 34) ÷ 2	= 360 5r = 324
x = 360 - 117 $x = 243^{\circ}$		x = 129°	$x = 64.8^{\circ}$
			Missing angles are 64.8° and 103.6°
9.	10.	11.	12.
<i>x</i> = (360 – 35 – 35 – 25 – 25) ÷ 2	180 - 80 = 100	<i>x</i> = 180 – 100 – 45	2 <i>x</i> + <i>x</i> + 135 + 135 = 360
x = 120°	y = 360 - 100 - 100 - 75 y = 85°	x = 35°	3 <i>x</i> = 90 <i>x</i> = 30°

### **Angles in Mixed Quadrilaterals - Expert**



### Angles in Mixed Quadrilaterals - Expert **Answers**

1. <b>360 - 214 = 146°</b>	2. 5 <i>x</i> - 4 + 2 <i>x</i> + <i>x</i> + 96 = 360	3. x = 180 - 100 - 45	4. <b>35 × 2 = 70</b>
x = 180 - 146 x = 34°	8x + 92 = 360 8x = 268 $x = 33.5^{\circ}$	x = 35°	2x - 3 + 2x - 3 + 2x - 3 + 2x - 3 + 35 + 35 + 35 + 35 = 360 8x = 232 x = 29
y = 180 - 63 y = 117°	Missing angles are 163.5°, 33.5° and 67°		$y = 360 - (4 \times 29 - 6)$ $y = 250^{\circ}$
5. <b>180 - 125 = 55°</b>	6. <b>3</b> <i>a</i> + <i>b</i> + <i>a</i> - <b>3</b> <i>b</i> = <b>180</b>	7. <b>180 - 68 = 112°</b>	8. <b>360 - 334 = 26°</b>
x = 360 - 55 x = 305°	4a - 2b = 180 3a + b = 110	3y + y + 48 + 112 + 90 = 360 4y + 250 = 360	360 - 132 = 228° 360 - 228 - 64 - 26 = 42
x = 303	<i>Su</i> · <i>b</i> = 110	4y = 110	<i>x</i> = 360 - 42
	<i>a</i> = 40	<i>y</i> = 27.5	<i>x</i> = 318°
	<i>b</i> = -10	Missing angles are 112°, 82.5° and 75.5°	
9. <b>180 - 80 = 100</b>	10. <b>360 - 318 = 42</b>	11. <b>2</b> <i>x</i> + <b>100</b> + <b>95</b> + <b>60</b> = <b>360</b>	12. <b>2</b> <i>x</i> + <b>4</b> + <i>x</i> + <i>y</i> + <b>90</b> = <b>360</b>
<i>y</i> = 360 – 100 – 100 – 75	(360 - 84 - 42) ÷ 2 = 117	2 <i>x</i> + 255 = 360	3x + y + 94 = 360
<i>y</i> = 85°	<i>x</i> = 360 – 117	2 <i>x</i> = 105	3x + y = 266
	<i>x</i> = 243°	<i>x</i> = 52.5°	
		Missing angle is 105°	x + y + 5 = 180 x + y = 175
			$x \cdot y = 1/3$
			2 <i>x</i> = 91
			<i>x</i> = 45.5°
			<i>y</i> = 129.5°

### **Angles in Parallelograms - Expert**



### Angles in Parallelograms - Expert **Answers**

		-		
1.		2.	3.	4.
	<i>x</i> = 180 – 64	180 – 77 = 103°	180 – 125 = 55°	4x + 110 = 180
	<i>x</i> = 116°			4x = 70
		x = 360 - 103	x = 360 - 55	x = 17.5
	$v = 64^{\circ}$	$x = 257^{\circ}$	$r = 305^{\circ}$	
	y on			z = 180 - 110
				z = 70°
				2 - 70
5.		6.	7.	8.
	2x + 3 + x = 180	2x + 12 + 5x = 180	17x - 5 + 8x = 180	180 – 105 = 75°
	3x = 177	7x = 168	25x = 185	
	$x = 59^{\circ}$	x = 24	x = 7.4	v + 75 = 180
				$y = 105^{\circ}$
	$v = 59 \times 2 + 3$	Missing angles are 120°	$8 \times 7 4 + 4y = 180$	y ios
	y = 33 × 2 + 3	and 60°	$A_{y} = 120.9$	
	<i>y</i> <b>–</b> 121		4y = 120.0	
			<i>y</i> <b>- 30.2</b>	
9.		10.	11.	12.
	<i>v</i> = 360 – 254	5x + 3x + 4 = 180	3a + b + a - 3b = 180	5 <i>v</i> + 115 = 180
	v = 106°	8 <i>x</i> = 176	4a - 2b = 180	5v = 65
	<i>.</i>	x = 22		v = 13
	10 <i>x</i> + 2 + 106 = 180		3a + b = 110	
	<b>10</b> <i>x</i> = <b>7</b> 2	Missing angles are		7x - 5 = 65
	<i>x</i> = <b>7.2</b>	110° and 70°	<i>a</i> = <b>40</b>	7x = 70
			<i>b</i> = -10	x = 10

### **Angles in Quadrilaterals - Expert**



### Angles in Quadrilaterals - Expert **Answers**

1. <b>360 – 214 = 146°</b>	2. <b>360 - 268 = 92°</b>	3. x = 71°	4. <b>180 - 58 = 122°</b>
x = 180 - 146 $x = 34^{\circ}$ y = 180 - 63 $y = 117^{\circ}$	x = 88° z = 92°	y = 180 - 71 y = 109°	x = 360 - 122 - 94 - 87 x = 57°
5. <b>180 - 121 = 59°</b> x = 360 - 100 - 84 - 59 x = 117°	6. $2x + 100 + 95 + 60 = 360$ 2x + 255 = 360 2x = 105 $x = 52.5^{\circ}$ Missing angle is 105°	7. $180 - 68 = 112^{\circ}$ 3y + y + 48 + 112 + 90 = 360 4y + 250 = 360 4y = 110 y = 27.5 Missing angles are 112°, $82.5^{\circ}$ and 75.5°	8. $5x - 5 + 2x + 3x + 90 = 360$ 10x + 85 = 360 10x = 275 x = 27.5 Missing angles are 132.5°, $55^{\circ}$ , 82.5°
9. $180 - 90 = 90^{\circ}$ $360 - 148 = 212^{\circ}$ $180 - 151 = 29^{\circ}$ x = 360 - 212 - 90 - 29 $x = 29^{\circ}$	10. $5x - 4 + 2x + x + 96 = 360$ 8x + 92 = 360 8x = 268 $x = 33.5^{\circ}$ Missing angles are 163.5°, $33.5^{\circ}$ and 67°	11. $360 - 334 = 26^{\circ}$ $360 - 132 = 228^{\circ}$ 360 - 228 - 64 - 26 = 42 x = 360 - 42 $x = 318^{\circ}$	12. $2x + 4 + x + y + 90 = 360$ 3x + y + 94 = 360 3x + y = 266 x + y + 5 = 180 x + y = 175 2x = 91 $x = 45.5^{\circ}$ $y = 129.5^{\circ}$

### **Angles in Rhombuses - Expert**



### Angles in Rhombuses - Expert **Answers**

1. $3x + x + 3x + x = 360$	2. 5x - 6 + x + 5x - 6 + x = 360	3. x = 123°	4. <i>x</i> = 132°
8 <i>x</i> = 360	12 <i>x</i> = 372	y = (360 – 123 – 123) ÷ 2	<i>y</i> = (360 – 132 – 132) ÷ 2
<i>x</i> = 45°	<i>x</i> = 31°	<i>y</i> = 57°	<i>y</i> = 48°
Missing angles are 45°, 45°,	Missing angles are 31°, 31°,	z = 360 – 57	z = 360 - 48
135° and 135°	149° and 149°	z = 303°	z = 312°
5. <b>360 - 307 = 53°</b>	6. <b>360 - 299 = 61°</b>	7. <b>23</b> <i>x</i> <b>- 5 + 14</b> <i>x</i> <b>+ 110 + 70 = 360</b>	8. 6x + 2x + 6x + 2x = 360
(360 – 53 – 53) ÷ 2 = 127°	(360 – 61 – 61) ÷ 2 = 119°	37 <i>x</i> = 185	16 <i>x</i> = 360
<i>x</i> = 360 – 127	<i>y</i> = 360 – 119	<i>x</i> = 5	<i>x</i> = 22.5
<i>x</i> = 233°	<i>y</i> = 241°	Or, solve to find the opposite angle.	
		23 <i>x</i> - 5 = 110	
		23 <i>x</i> = 115	
		<i>x</i> = 5	
9. x = 115°	10. <b>40 × 2 = 80</b>	11. <b>26 × 2 = 52</b>	12. <b>35 × 2 = 70</b>
2 <i>y</i> + 2 <i>y</i> + 115 + 115 = 360	<i>x</i> = (360 – 80 – 80) ÷ 2	5x - 2 + 5x - 2 + 52 + 52 = 360	2x - 3 + 2x - 3 + 2x - 3 + 2x - 3 +
4 <i>y</i> = 130	<i>x</i> = 100°	10 <i>x</i> = 260	35 + 35 + 35 + 35 = 360
<i>y</i> = 32.5	<i>y</i> = 360 – 100	<i>x</i> = 26	8x = 232
z = 360 - (32.5 × 2)	<i>y</i> = 260°	y = 360 - (5 × 26 - 2)	<i>x</i> = 29
z = 295°		y = 232°	$y = 360 - (4 \times 29 - 6)$
			<i>y</i> = 250°

#### **Colour by Number: Angles in Quadrilaterals - Expert**

Each question gives information about the interior angles of a quadrilateral. Calculate the value of *x* then use the key to shade the section in the correct colour.



	·
	Question
1.	right angle, 2 <i>x</i> – 50°, 71°, 57°
2.	<i>x</i> – 72°, <i>x</i> – 72°, 57°, 45°
3.	2 <i>x</i> – 100°, 18°, 32°, 8°
4.	196°, 2 <i>x</i> , <i>x</i> , 68°
5.	<i>x</i> + 10°, <i>x</i> + 10°, 118°, 118°
6.	right angle, 15°, 30°, <i>x</i>
7.	3 <i>x</i> – 26°, right angle, 5°, 12°
8.	4x
9.	215°, 75°, 38°, <i>x</i>
10.	<i>x</i> + 61°, <i>x</i> + 61°, 36°, 10°
11.	right angle, 135°, 45°, x

12. | 142°, *x*, 100°, 30°

13.	2 <i>x</i> + 5°, 2 <i>x</i> + 5°, 81°, 81°
14.	175°, 111°, 43°, <i>x</i>
15.	right angle, 212°, 38°, <i>x</i>
16.	3 <i>x</i> – 50°, 65°, 51°, 24°
17.	95°, 95°, <i>x</i> , <i>x</i>
18.	2 <i>x</i> , 2 <i>x</i> , 100°,100°
19.	right angle, 123°, 79°, <i>x</i>
20.	3 <i>x</i> – 4°, 3 <i>x</i> – 4°, 43°, 43°
21.	2 <i>x</i> – 15°, 2 <i>x</i> – 15°, 13°, 13°
22.	125°, 125°, <i>x</i> , <i>x</i>
23.	104°, 42°, 58°, <i>x</i>
24.	153°, 153°, 10°, <i>x</i>
25.	114°, 32°, 23°, <i>x</i>
26.	156°, 100°, 14°, <i>x</i>
27.	36°, 51°, 23°, <i>x</i>
28.	right angle, 97°, 84°, <i>x</i>
29.	61°, 35°, 172°, <i>x</i>
30.	105°, 105°, 98°, <i>x</i>
31.	<i>x</i> – 56°, <i>x</i> – 56°, 34°, 34°
32.	<i>x</i> + 7°, <i>x</i> + 7°, 88°, 88°
33.	2 <i>x</i> – 15°, 2 <i>x</i> – 15°, 21°, 9°
34.	x – 12°, x – 12°, 111°, 111°
35.	2 <i>x</i> – 8°, 2 <i>x</i> – 8°, 38°, 38°
36.	115°, 115°, <i>x</i> , <i>x</i>
37.	75°, 48°, 39°, <i>x</i>
38.	115°, 57°, 96°, <i>x</i>
39.	107°, 100°, 65°, <i>x</i>
40.	120°, 120°, <i>x</i> , <i>x</i>
41.	152°, 60°, 64°, <i>x</i>
42.	2 <i>x</i> – 350°, 2 <i>x</i> – 350°, 110°, 110°
43.	150°, 150°, 45°, <i>x</i>
44.	5 <i>x</i> – 4°, 5 <i>x</i> – 4°, 58°, 10°
45.	92°, 92°, <i>x</i> , <i>x</i>
46.	2 <i>x</i> + 10°, 2 <i>x</i> + 10°, 146°, 70°
47.	112°, 95°, 64°, <i>x</i>
48.	2 <i>x</i> – 35°, 2 <i>x</i> – 35°, 56°, 14°
49.	<i>x</i> + 17°, <i>x</i> + 17°, 98°, 48°
50.	95°, 101°, 72°, <i>x</i>

#### Colour by Number: Angles in Quadrilaterals - Expert Answers

Each question gives information about the interior angles of a quadrilateral. Calculate the value of *x* then use the key to shade the section in the correct colour.



	Colour	Question
1.		right angle, 2 <i>x</i> – 50°, 71°, 57°
2.		<i>x</i> – 72°, <i>x</i> – 72°, 57°, 45°
3.		2 <i>x</i> – 100°, 18°, 32°, 8°
4.		196°, 2 <i>x</i> , <i>x</i> , 68°
5.		<i>x</i> + 10°, <i>x</i> + 10°, 118°, 118°
6.		right angle, 15°, 30°, <i>x</i>
7.		3 <i>x</i> – 26°, right angle, 5°, 12°
8.		4x
9.		215°, 75°, 38°, <i>x</i>
10.		<i>x</i> + 61°, <i>x</i> + 61°, 36°, 10°
11.		right angle, 135°, 45°, <i>x</i>
12.		142°, <i>x</i> , 100°, 30°

#### Colour by Number: Angles in Quadrilaterals - Expert **Answers**

13.	2 <i>x</i> + 5°, 2 <i>x</i> + 5°, 81°, 81°
14.	175°, 111°, 43°, <i>x</i>
15.	right angle, 212°, 38°, <i>x</i>
16.	3 <i>x</i> – 50°, 65°, 51°, 24°
17.	95°, 95°, <i>x</i> , <i>x</i>
18.	2 <i>x</i> , 2 <i>x</i> , 100°,100°
19.	right angle, 123°, 79°, <i>x</i>
20.	$3x - 4^{\circ}, 3x - 4^{\circ}, 43^{\circ}, 43^{\circ}$
21.	2 <i>x</i> – 15°, 2 <i>x</i> – 15°, 13°, 13°
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27.	36°, 51°, 23°, <i>x</i>
28.	right angle, 97°, 84°, <i>x</i>
29.	61°, 35°, 172°, <i>x</i>
30.	105°, 105°, 98°, <i>x</i>
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37.	75°, 48°, 39°, <i>x</i>
38.	115°, 57°, 96°, <i>x</i>
39.	107°, 100°, 65°, <i>x</i>
40.	120°, 120°, <i>x</i> , <i>x</i>
41.	152°, 60°, 64°, <i>x</i>
42.	2 <i>x</i> – 350°, 2 <i>x</i> – 350°, 110°, 110°
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44.	5 <i>x</i> – 4°, 5 <i>x</i> – 4°, 58°, 10°
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48.	2 <i>x</i> – 35°, 2 <i>x</i> – 35°, 56°, 14°
49.	<i>x</i> + 17°, <i>x</i> + 17°, 98°, 48°
50.	95°, 101°, 72°, <i>x</i>

### **Angles in Quadrilaterals - Essential**

Solve the clues to find the four-digit code to escape the classroom!



The first digit of the code is given by the tenths in the value of x in question 1. The second digit is given by the tens digit in the answer to question 2. The third digit is given by the sum of the digits of angle x in question 3. The fourth digit is the sum of the digits of y in question 4.



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#### Angles in Quadrilaterals - Essential **Answers**

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1. <b>360 - 245 = 115</b> °	2. $5x + x + 5x + x = 360$
	12 <i>x</i> = 360
<i>y</i> = 115°	<i>x</i> = 30°
8x + 5 + 115 = 180	
8 <i>x</i> = 60	
<i>x</i> = 7.5	
3. x = 360 - 112 - 112 - 35	4. <b>180 - 70 = 110°</b>
<i>x</i> = 101°	4 <i>y</i> + <i>y</i> + 57 + 90 + 110 = 360
	5 <i>y</i> = 103
	<i>y</i> <b>= 20.6</b>

Exit Code: 5328

### **Angles in Quadrilaterals - Expert**

Solve the clues to find the four-digit code to escape the classroom!



The first digit of the code is given by the sum of the digits for angle x in question 1. The second digit is given by the units for both x and y in question 2. The third digit is given by the tens in the value for x in question 3. The fourth digit is given by the units in the value for x in question 4.



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#### Angles in Quadrilaterals - Expert **Answers**

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The first digit of the code is given by the sum of the digits for angle x in question 1. The second digit is given by the units for both x and y in question 2. The third digit is given by the tens in the value for x in question 3. The fourth digit is given by the units in the value for x in question 4.



1. <b>360 - 320 = 40</b> °	2. 50 × 2 = 100°
(360 – 82 – 40) ÷ 2 = 119°	<i>x</i> = (360 – 100 – 100) ÷ 2
<i>x</i> = 360 – 119	<i>x</i> = 80°
<i>x</i> = 241°	
	y = 360 - 80
	y = 280°
3. 5 <i>x</i> - 15 + 10 <i>x</i> = 180	4. 2 <i>x</i> + <i>x</i> + 49 + 38 = 360
15 <i>x</i> = 195	3 <i>x</i> = 273
<i>x</i> = 13	x = 91°

Exit Code: 7011



#### Irregular Trapezium

#### **Properties:**

- The interior angles add up to 360°.
- Each angle may be different.
- It has 1 pair of parallel lines.
- It has 2 pairs of angles that are supplementary: they add up to 180°.



#### isosceles trapez

#### **Properties:**

- The interior angles add up to 360°.
- It has 1 pair of parallel lines.
- There are 2 pairs of angles that are equal.
- Both pairs of opposite angles are supplementary: they add up to 180°.



#### Square

#### **Properties:**

- The interior angles add up to 360°.
- Each angle is 90°.
- All sides have equal length.
- It has 2 pairs of parallel lines.



#### **Properties:**

- The interior angles add up to 360°.
- All sides have equal length.
- Opposite sides are parallel and opposite angles are equal.
- The diagonals bisect each other at a right angle.

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- Properties:The interior angles add up to 360°.
- There are 2 congruent pairs of sides.
- Each pair consists of 2 equal-length sides that are adjacent (they meet).
- The angles are equal where the 2 pairs meet.
- The diagonals are perpendicular.



#### Parallelogram

- The interior angles add up to 360°.
- Opposite sides are parallel.
- Opposite sides are equal in length.
- Opposite angles are equal (angles *a* are the same and angles *b* are the same).
- Angles *a* and *b* are supplementary: they add up to 180°.



- The interior angles add up to 360°.
- Each angle may be different.
- It has 1 pair of parallel lines.
- It has 2 pairs of angles that are supplementary: they add up to 180°.



- The interior angles add up to 360°.
- Each angle is 90°.
- All sides have equal length.
- It has 2 pairs of parallel lines.



- •The interior angles add up to 360°.
- •There are 2 congruent pairs of sides.
- •Each pair consists of 2 equal-length sides that are adjacent (they meet).
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- •The diagonals are perpendicular.



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- The interior angles add up to 360°.
- Opposite sides are parallel.
- Opposite sides are equal in length.
- Opposite angles are equal (angles *a* are the same and angles *b* are the same).
- Angles *a* and *b* are supplementary: they add up to 180°.

### Angle Properties Angles in Quadrilaterals: Expert Level



## **Learning Objective**

To identify and find missing angles in quadrilaterals. Targeting Assessment Objectives AO1 and AO2

### **Success Criteria**

- To recall the key properties of different quadrilaterals.
- To use an angle rule to find a missing value.
- Form and solve equations using knowledge of angle facts.

# **Starter Task**

Think, Pair, Share

Write down the definition of a quadrilateral.

A quadrilateral is a twodimensional, four-sided shape which is closed (the lines join up) and has straight sides. List some examples of quadrilaterals.

Some examples include square, rectangle, trapezium, rhombus, parallelogram and kite.

List some of the properties of a quadrilateral.

- four sides (edges)
- four corners (vertices)
- interior angles that add up to 360°

Draw an example of a quadrilateral.

# Quadrilaterals

A quadrilateral is a two-dimensional, four-sided shaped which is closed (the lines join up) and has straight sides.

The interior angles of a quadrilateral always sum to 360°.

# Quadrilaterals

Using the angles in each question, decide whether it is a quadrilateral or not.

	<b>√</b> Quadrilateral	X Not a Quadrilateral
56°, 131°, 95°, 108°		×
90°, 160°, 75°, 35°	✓	
115°, 37°, 185°, 23°	~	- / /
237°, 102°, 14°, 7°	~ ~	
96°, 48°, 145°, 72°		×
116°, 116°, 98°, 30°		- Alexer /



# Square

The interior angles add up to 360°.

Each angle is 90°.

All sides have equal length.

It has 2 pairs of parallel lines.



# Rectangle

The interior angles add up to 360°. Each angle is 90°. It has 2 pairs of equal angles.

It has 2 pairs of parallel lines.



### Irregular Trapezium

The interior angles add up to 360°.

Each angle may be different.

It has 1 pair of parallel lines.

It has 2 pairs of angles that are supplementary: they add up to 180°.



### **Isosceles Trapezium**

The interior angles add up to 360°.

It has 1 pair of parallel lines.

There are 2 pairs of angles that are equal.

Both pairs of opposite angles are supplementary: they add up to 180°.



### Rhombus

The interior angles add up to 360°.

All sides have equal length.

Opposite sides are parallel and opposite angles are equal.

The diagonals bisect each other at right angle.

### Parallelogram



Opposite sides are parallel.

Opposite sides are equal in length

Opposite angles are equal (angles *a* are the same and angles *b* are the same).

Angles *a* and *b* are supplementary: they add up to  $180^{\circ}$ .

h

00°

100°

### Kite



There are 2 congruent pairs of sides.

Each pair consists of 2 equal-length sides that are adjacent (they meet).

The angles are equal where the 2 pairs meet.

The diagonals are perpendicular.

Find the value of *x*. Hence, find all the missing angles.



6x - 3 + 2x + x + 111 = 360

**9***x* = **252** 

*x* = 28°

Missing angles are 28°, 56° and 165°

Find the value of *x*. Hence, find all the missing angles.



5x + 2 + 4x + x + 98 = 360

10x = 260

*x* = 26°

Missing angles are 26°, 104° and 132°

Find the value of *x*. Hence, find all the missing angles.



3x - 32 + 3x - 32 + x + 67 = 3607x = 357 $x = 51^{\circ}$ 

Missing angles are 51°, 121° and 121°

Find the value of *x*. Hence, find all the missing angles. Give a reason for each stage of your working.



**1**80 – 126 = 54°

2x - 15 + 3x + x + 54 = 360

Angles on a straight line add up to 180° Angles in a quadrilateral add up to 360°

6*x* = 321

*x* = 53.5°

Missing angles are 54°, 53.5°, 160.5° and 92°



# **Escape the Room**



#### Angles in Quadrilaterals - Expert

Solve the clues to find the four-digit code to escape the classroom!





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x in question 4.





#### Angles in Quadrilaterals Teaching Ideas

#### Learning Objective:

To identify and find missing angles in quadrilaterals.

Targeting Assessment Objectives AO1 and AO2.

#### **Success Criteria:**

- To recall the key properties of different quadrilaterals.
- To use an angle rule to find a missing value.
- Form and solve equations using knowledge of angle facts.

#### Context

This lesson aims to secure students' understanding of how to find missing angles in a range of quadrilaterals. The lesson aims to extend students' learning by requiring them to use an algebraic method to find the missing angles in a quadrilateral. Therefore, they should have a good understanding of how to calculate angles on a straight line and about a point as well as how to form and solve equations (including a few simultaneous equations for additional challenge).

#### Resources

- PowerPoint
- Angles in Quadrilaterals
- Angles in Kites
- Angles in Rhombuses
- Angles in Parallelograms
- Angles in Mixed Quadrilaterals

#### Starter

#### Think, Pair, Share

Display the 'Think, Pair, Share' questions. Allow students approximately 5 minutes to discuss their ideas with a partner. They could record their answers in books or mini-whiteboards.

#### Main Activities

#### Quadrilaterals

Once the starter is completed, draw the class together to talk through their ideas. Using the following slide, share the main teaching point that interior angles of a quadrilateral always add up to 360 degrees. Students should record this in their books. Following this, students are asked to apply their understanding to decide whether the angles make a quadrilateral or not. When asking for the answers, ensure you clarify students' understanding by asking them why it can't be a quadrilateral. Answers should be focusing on the interior angles in a quadrilateral adding up to 360 degrees.

#### **Types of Quadrilaterals**

The following slides go through each key quadrilateral and share the key properties for each. These are also available as posters if you don't wish for students to copy down from the board. You could also refer to the images on each slide when discussing the properties to highlight them.

#### **Finding Missing Angles in Quadrilaterals**

All the examples are designed to guide students on how to calculate the missing angle in a quadrilateral. Each slide provides a question followed by the calculations broken down into simple steps. You may wish to simply display the question and ask students for suggestions for the missing angles via whole class discussion. Alternatively, you may wish for students to work independently on the questions and display their answers on mini-whiteboards. Either way, encourage students to use the angle rule (that the angles in a quadrilateral add up to 360 degrees) to justify their answer by asking them, 'why is your answer correct?' 'Why can't the answer be something else?' You may wish for students to record their answers and calculations in their books.

Following this, students have the option of completing a range of **Angles in Quadrilaterals Worksheets**. They can focus on a particular quadrilateral or they may wish to complete the mixed quadrilateral sheet. Alternatively, students may also choose the Colour by Number activity to help them practise finding missing angles in quadrilaterals.

- Colour by Number
- Angles in Quadrilaterals Posters
- Escape the Room Essential
- Escape the Room Expert

#### Plenary

The plenary draws the lesson together by asking students to reflect on their learning during the lesson. Allow students enough time to complete the three questions. Use your best judgement to decide whether students share what they've written with the class or whether you will read them afterwards.

#### **Escape the Room**

**Escape the Room** requires students to find missing angles in four quadrilaterals to find a code to 'exit' the room at the end of the lesson. These are differentiated at two different levels. You may wish for students to pass you their answers on leaving the classroom as they may provide you with immediate information that you can use to assess students' understanding and provide insight for subsequent lessons.